

## 58093 String Processing Algorithms (Autumn 2010)

### Exercises 5 (9 December)

1. Let  $T = \text{lallilla}\$$ .
  - (a) Give the suffix tree of  $T$  including suffix links.
  - (b) Give the suffix array of  $T$  together with the LCP array.
2. Write a pseudocode algorithm for finding all occurrences of a pattern  $P$  in a text  $T$  using the suffix tree of  $T$ .
3. The reverse of a string  $S[0..m)$  is the string  $S^R = S[m-1]S[m-2]..S[0]$ . Describe an algorithm for finding the longest factor  $S$  of  $T$  such that the reverse  $S^R$  is a factor of  $T$  too. The method should work in linear time.
4. Give a linear time algorithm for computing the matching statistics of  $T$  with respect to  $S$  from the generalized suffix array of  $S$  and  $T$  and the associated LCP array (without constructing the suffix tree).
5. Hamming distance is the edit distance with substitution as the only allowed edit operation. Let  $ed_H(A, B)$  denote the Hamming distance of two strings  $A$  and  $B$  of the same length.
  - (a) Suppose we have preprocessed the strings  $A$  and  $B$  so that the longest common extension for any pair of suffixes can be computed in constant time. Show how the Hamming distance  $ed_H(A, B)$  can be computed in  $\mathcal{O}(ed_H(A, B))$  time.
  - (b) Design an  $\mathcal{O}(kn)$  worst case time algorithm for approximate string matching with Hamming distance.
6. Prove Lemma 4.9. *Hint:* Generalize Lemma 3.17(b) (Lecture 6) from three strings to many strings.
7. What is the number of distinct factors in the string `abracadabra`?
8. Fill the course feedback form at <https://ilmo.cs.helsinki.fi/kurssit/servlet/Valinta?kieli=en>