

# Pakota: A System for Enforcement in Abstract Argumentation

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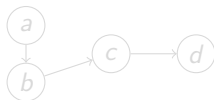
# Motivation

## Argumentation

- An active area of modern AI research
- Connections to logic, philosophy, and law
- Applications: decision support, legal reasoning, medical diagnostics, etc.

## Dung's argumentation frameworks (AFs)

- Central KR formalism in **abstract argumentation**
- Recent interest in **dynamic aspects** of AFs
  - ▶ E.g., how to adjust a given AF in light of new knowledge?



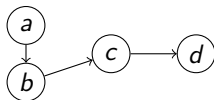
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## Pakota

System for solving enforcement via employing MaxSAT and SAT solvers.

- **Describe** the system in detail
  - ▶ System architecture overview
  - ▶ Features
    - ★ Supported semantics and problem variants
    - ★ MaxSAT and SAT solver interfaces
  - ▶ Algorithms
    - ★ Problems in NP: direct MaxSAT encodings
    - ★ Beyond NP: MaxSAT-based CEGAR procedures
  - ▶ Input format, usage and options
- **Provide** benchmarks and generators for enforcement
- **Evaluate** the impact of the choice of the MaxSAT solver on scalability

# Argumentation Frameworks

## Syntax

An argumentation framework (AF) is a directed graph  $F = (A, R)$ , where

- $A$  is the set of **arguments**
- $R \subseteq A \times A$  is the **attack relation**
  - ▶  $a \rightarrow b$  means argument  $a$  attacks argument  $b$

## Semantics

Define sets of jointly accepted arguments or **extensions**

- a function  $\sigma$  mapping an AF  $F = (A, R)$  to a collection  $\sigma(F) \subseteq 2^A$
- e.g. **conflict-free**:  $E \in cf(F)$  if  $E$  is an independent set

## Acceptability of arguments

Given an AF  $F = (A, R)$  and semantics  $\sigma$ , an argument  $a \in A$  is

- **credulously** accepted under  $\sigma$  iff  $a$  is in **some** extension
- **skeptically** accepted under  $\sigma$  iff  $a$  is in **all** extensions

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# AF Reasoning Tasks

## Static computational problems

Direct inference from a given AF—no change involved

- credulous and skeptical acceptance of an argument
- extension enumeration

Many system implementations available!

## Dynamic computational problems

How to change a given AF to support new information?

## Pakota

First system implementation in its generality for solving instances of

- extension enforcement
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# Extension Enforcement

## Problem definition

[Coste-Marquis et al., 2015; Wallner et al., 2016]

- Input: AF  $F = (A, R)$ ,  $T \subseteq A$ , semantics  $\sigma$
- Task: Find an AF  $F' = (A, R')$  such that
  - ▶  $T \in \sigma(F')$  (**strict** extension enforcement)
  - ▶  $T \subseteq T' \in \sigma(F')$  (**non-strict** extension enforcement)

and the number of changes  $|R \Delta R'|$  is minimized.

## Example

Enforcing  $T = \{a\}$  strictly under the preferred semantics.



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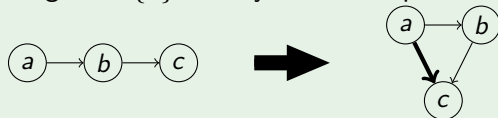
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# Status Enforcement

## Credulous status enforcement

[Niskanen et al., 2016]

- Input: AF  $F = (A, R)$ , disjoint sets  $P, N \subseteq A$ , semantics  $\sigma$
- Task: Find an AF  $F' = (A, R')$  such that
  - ▶ all arguments in  $P$  are **credulously** accepted
  - ▶ all arguments in  $N$  are not **credulously** acceptedand the number of changes  $|R \Delta R'|$  is minimized.

## Skeptical status enforcement

[Niskanen et al., 2016]

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# Computational Complexity of Enforcement

**Table:** Complexity of extension and status enforcement.

[Wallner et al., 2016; Niskanen et al., 2016]

	extension enf.		status enf. ( $N = \emptyset$ )		status enf. (unrestr. case)	
$\sigma$	strict	non-strict	credulous	skeptical	credulous	skeptical
<i>cf</i>	in P	in P	in P	trivial	in P	trivial
<i>adm</i>	<b>in P</b>	<b>NP-c</b>	<b>NP-c</b>	trivial	$\Sigma_2^P$ -c	trivial
<i>stb</i>	<b>in P</b>	<b>NP-c</b>	<b>NP-c</b>	$\Sigma_2^P$ -c	$\Sigma_2^P$ -c	$\Sigma_2^P$ -c
<i>com</i>	<b>NP-c</b>	<b>NP-c</b>	<b>NP-c</b>	NP-c	$\Sigma_2^P$ -c	NP-c
<i>prf</i>	$\Sigma_2^P$ -c	<b>NP-c</b>	<b>NP-c</b>	in $\Sigma_3^P$	$\Sigma_2^P$ -c	in $\Sigma_3^P$

## Features of the system

- Employs MaxSAT and SAT solvers for solving enforcement instances
- Allows for optimally solving
  - ▶ extension enforcement under  $\sigma \in \{adm, com, stb, prf\}$
  - ▶ credulous status enforcement under  $\sigma \in \{adm, com, stb, prf\}$
  - ▶ skeptical status enforcement under  $\sigma \in \{adm, stb\}$
- Offers an interface for plugging in the MaxSAT solver of choice
- Output of MaxSAT encodings in standard WCNF and LP formats



# Enforcement via Maximum Satisfiability

## The (partial) maximum satisfiability problem

- **Input:** Hard clauses  $\varphi_h$  and soft clauses  $\varphi_s$
- **Task:** Find a truth assignment that satisfies **all** hard clauses and **as many** soft clauses as possible

Used as a declarative language for solving optimization problems in NP.

## NP-encodings

- Soft clauses encode **modifications** to the attack structure
- Hard clauses encode the **properties** of enforcement

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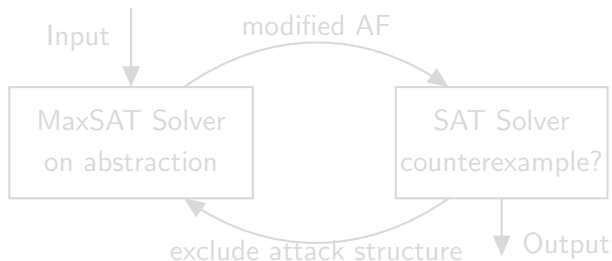
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# Counterexample-Guided Abstraction Refinement

## Beyond NP: Counterexample-guided abstraction refinement (CEGAR)

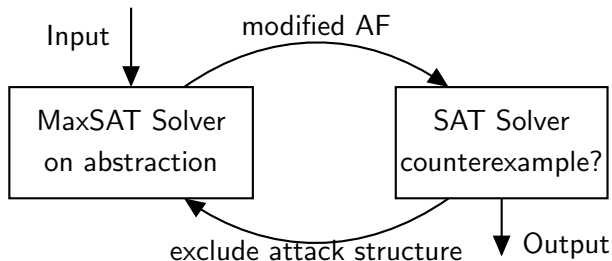
- **Start** with a **NP-abstraction**, solved using a MaxSAT solver
  - ▶ Lower bound on the cost of the solution
- **Refine** using a **counterexample**, provided by a SAT solver, until no counterexample is found
  - ▶ SAT check on the validity of the solution



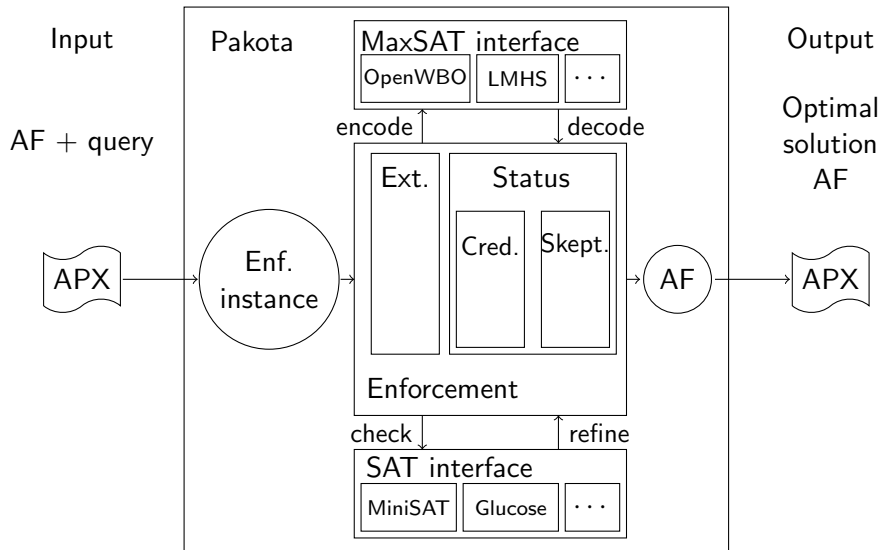
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# System Architecture



# Performance Overview: First Level

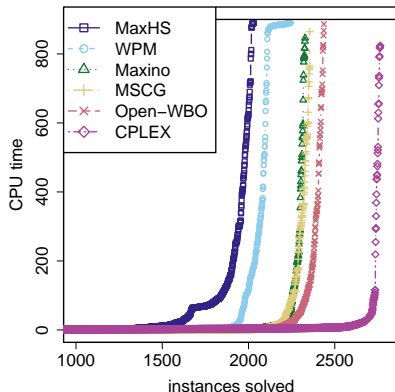
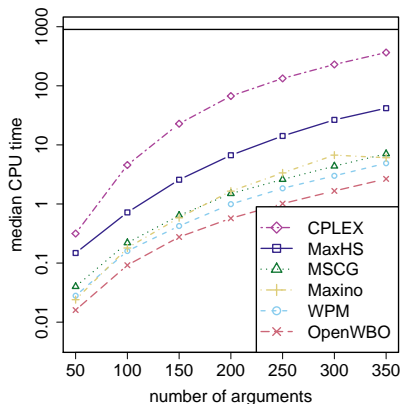


Figure: MaxSAT solver comparison on NP-complete extension enforcement; Left: strict enf. under complete; right: non-strict enf. under stable

# Performance Overview: Second Level

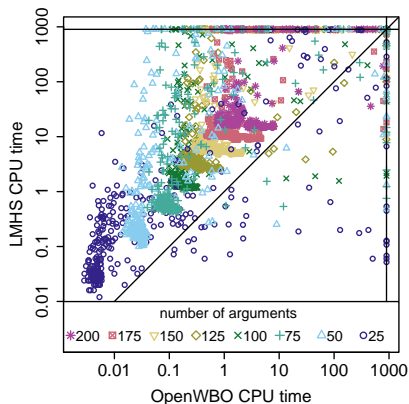
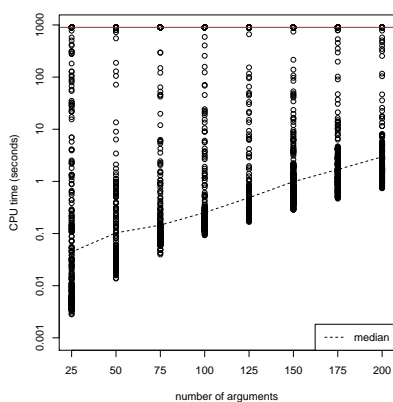


Figure: MaxSAT solver comparison on  $\Sigma_2^P$ -complete extension enforcement; Strict enforcement under preferred

# Paper Summary

## Pakota

- The first system implementation in its generality for solving problem instances of extension and status enforcement
- Utilizes MaxSAT solvers directly for the NP-complete variants and a CEGAR procedure for the problems beyond NP

## Contributions

- Overview of the Pakota system:
  - ▶ System architecture and features
  - ▶ Details on encodings and algorithms
  - ▶ More in paper!
- Empirical evaluation of the impact of the choice of MaxSAT solvers
- System available online under an open source licence:  
<http://www.cs.helsinki.fi/group/coreo/pakota/>
- Future: Extending the system to support further central AF semantics



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# References

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Thank you for your attention!